Michigan Math Club Thursday at 4pm in the Nesbitt Room Free Pizza and Pop

Polynomial Roots modulo Prime Perfect Squares

Robert Walker

Abstract for 12 October

Fix a univariate polynomial f(x) with integer coefficients, and a prime integer P not dividing every coefficient of f(x). Can you give a simple formula for the number of solutions to f(x) = 0 modulo P^k for any positive integer k? When k=1, this is a benign task with ties to Fermat's Little Theorem. Until 2017, however, it was unknown whether this was feasible modulo P^2 (or P^3, P^4,...). Three REU students I advised figured out how to do this. The talk will work up to presenting their formula.