## Michigan Math Club

Meeting <u>virtually</u> for Fall 2020 Thursdays at 4pm EDT

## Conway's topographs

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 $24 \ {\rm September} \ 2020$ 

In the 1990s, John H. Conway developed a new way of seeing binary quadratic forms. Binary quadratic forms are functions, like  $Q(x,y) = x^2 + 7xy - 3y^2$  which are allowed only integer inputs. Each binary quadratic form can be depicted, through Conway's "topograph," as a map of numbers drawn on the hyperbolic plane. By associating the number 0 with "water," one can see things like the infinitude of solutions to the equation  $x^2 - 3y^2 = 1$  just by "following the river." I will try to pay homage to Conway, by introducing his topograph and some generalizations that have shaped my research.

