Michigan Math Club Thursday at 4pm in the Nesbitt Room Free Pizza and Pop

Impossibility theorems for elementary integration

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Abstract for 19 January



The error function and logarithmic integral, defined by

$$\operatorname{erf}(x) = \int_0^x e^{-t^2} dt$$
 $\operatorname{Li}(x) = \int_2^x \frac{1}{\ln(t)} dt$,

are two very important functions within mathematics. However, they cannot be expressed in terms of elementary functions. We will provide a proof of this fact using a criterion of B. Conrad, which in turn is based on a theorem by Liouville.