1. An enterprising calculus student determines that for a particularly interesting (it is, after all, on a quiz) function g(x), $\int_1^5 g(x) dx = 3$, g(1) = 1, and g(5) = 2. If possible, find $\int_1^5 x g(x^2 + 4) dx$ (if it isn't possible, explain why). (3 points)

2. For the same tremendously interesting function g(x) given in problem (1), find, if possible, $\int_1^5 x g'(x) dx$ (if it isn't possible, explain why). (3 points)

3. Let the function $f(x) = \int_0^{\cos(x)} \sin(t^2) dt + 2$. What is the slope of the tangent line to f(x) at $x = \frac{\pi}{4}$? Find an estimate for the value of $f(\frac{\pi}{4})$ and use this to write an equation for the tangent line. (4 points)