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1. Supposed that a child's throwing toy is (essentially) a two-dimensional piece of plastic lying within $r=6 \theta \sin (\theta)$ (where $r$ is measured in inches), for $0 \leq \theta \leq \pi$. Find the surface area of the toy (the use of numerical integration is fine). (3 points)
2. Now, suppose that the density of the toy is given to be $\delta(\theta)=1+\frac{\theta}{2} \mathrm{~g} / \mathrm{in}^{2}$. Find the mass of the toy. (Again, using numerical integration is fine.) (3 points)
3. Set up but do not evaluate an expression to find the $y$-center of mass of a 2 inch wide by 3 inch high rectangular object having a density $\delta(y)=\cos (y) \mathrm{g} / \mathrm{in}^{2} .(y$ is the vertical coordinate, which measures the height of the object.) (4 points)
