

Name: \_\_\_\_\_ Score (Out of 7 points):

1. (3 points) Let  $(X, \mathcal{T}_X)$  be a topological space and let  $S \subseteq X$  be a subset endowed with the subspace topology  $\mathcal{T}_S$ . Suppose that  $X$  is Hausdorff. Show that  $S$  is Hausdorff.

2. (4 points) Let  $X$  and  $Y$  be topological spaces, and let  $f : X \rightarrow Y$  be a continuous **injective** map. Show that, if  $Y$  is Hausdorff, then  $X$  is Hausdorff.