

Name: \_\_\_\_\_ Score (Out of 7 points):

1. Let  $X$  be a nonempty finite set, say,  $X = \{x_1, x_2, \dots, x_n\}$  for some  $n \in \mathbb{N}$ . Let  $d$  be a metric on  $X$ .

(a) (4 points) Prove that, for any point  $x_i \in X$ , the singleton set  $U = \{x_i\}$  is open.

(b) (2 points) Prove that *every* subset  $U \subseteq X$  is open.

*Hint:* Write  $U$  as a union of singleton sets.

(c) (1 point) Prove that every subset  $U \subseteq X$  is closed.