

**Problem # 3.** Letting  $X = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ , we get

$$\begin{bmatrix} 1 & 3 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} 1 & 3 \\ 0 & 1 \end{bmatrix},$$

that is,

$$\begin{bmatrix} a + 3c & b + 3d \\ c & d \end{bmatrix} = \begin{bmatrix} a & 3a + b \\ c & 3c + d \end{bmatrix},$$

from which we get the system of linear equations

$$\begin{aligned} a + 3c &= a \\ b + 3d &= 3a + b \\ c &= c \\ d &= 3c + d. \end{aligned}$$

Solving the system, we get  $c = 0$ ,  $d = a$ , where  $a$  and  $b$  can be any numbers.

**Answer:**  $X = \begin{bmatrix} a & b \\ 0 & a \end{bmatrix}$ , where  $a$  and  $b$  can be any numbers.