**1.** Let A be the matrix of a linear transformation  $\mathbb{R}^3 \longrightarrow \mathbb{R}^3$  that is the orthogonal projection onto a plane in  $\mathbb{R}^3$ . Find the rank of A.

**Solution.** The rank of A is equal to the dimension of the image of A. The image of the orthogonal projection onto a plane is the plane.



Therefore, the rank of A is equal to the dimension of the plane, which is 2.

Answer. rank A = 2.