

# MATH 116 — PRACTICE FOR EXAM 3

Generated October 24, 2017

NAME: \_\_\_\_\_

INSTRUCTOR: \_\_\_\_\_ SECTION NUMBER: \_\_\_\_\_

---

1. This exam has 4 questions. Note that the problems are not of equal difficulty, so you may want to skip over and return to a problem on which you are stuck.
2. Do not separate the pages of the exam. If any pages do become separated, write your name on them and point them out to your instructor when you hand in the exam.
3. Please read the instructions for each individual exercise carefully. One of the skills being tested on this exam is your ability to interpret questions, so instructors will not answer questions about exam problems during the exam.
4. Show an appropriate amount of work (including appropriate explanation) for each exercise so that the graders can see not only the answer but also how you obtained it. Include units in your answers where appropriate.
5. You may use any calculator except a TI-92 (or other calculator with a full alphanumeric keypad). However, you must show work for any calculation which we have learned how to do in this course. You are also allowed two sides of a  $3'' \times 5''$  note card.
6. If you use graphs or tables to obtain an answer, be certain to include an explanation and sketch of the graph, and to write out the entries of the table that you use.
7. You must use the methods learned in this course to solve all problems.

Semester	Exam	Problem	Name	Points	Score
Fall 2014	3	4	robot army	8	
Winter 2012	3	10	drug	9	
Fall 2011	3	4	savings	9	
Winter 2011	3	4	signal fire	8	
Total				34	

**Recommended time (based on points): 41 minutes**

4. [8 points] Franklin's robots start building more robots to replace their deactivated comrades. The initial number of robots in Franklin's army is 800. Each minute, the number of robots increases by 15%. At the end of each minute, you fire an EMP which immediately deactivates 50 robots.
- a. [3 points] Let  $R_n$  denote the number of active robots in Franklin's army immediately after the EMP is fired for the  $n$ -th time. Find  $R_1$  and  $R_2$ .
- b. [4 points] Find a closed form expression for  $R_n$  (i.e. evaluate any sums and solve any recursion).
- c. [1 point] Find  $\lim_{n \rightarrow \infty} R_n$ . No justification is necessary.

10. [9 points] A patient takes a drug in doses of 100 mg once every 24 hours. The half-life of the drug in the patient's body is 12 hours. Let  $D_n$  be the amount of the drug in the patient immediately after taking the  $n$ th dose of the drug. Be sure to include units.

a. [3 points] Find  $D_1$ ,  $D_2$  and  $D_3$ .

b. [4 points] Find a closed form expression (an expression that does not involve a long summation or a recursive formula) for  $D_n$ .

c. [2 points] What is  $\lim_{n \rightarrow \infty} D_n$ ?

4. [9 points] Ramon starts depositing \$10,000 each year at his 25th birthday into a retirement account and continues until his 45th birthday. After this point, he does not touch the account until he is 65. The retirement account accrues interest at a rate of 3% compounded annually.
- a. [3 points] Let  $R_n$  be the amount of money *in thousands* of dollars in Ramon's retirement account after  $n$  years from his initial deposit. Find an expression for  $R_0$ ,  $R_1$  and  $R_2$ .
- b. [3 points] Find a closed form expression (an expression that does not involve a long summation) for how much money Ramon has in his retirement account at his 45th birthday.
- c. [3 points] Find a closed form expression for how much money Ramon has in his retirement account when he is 65 years old. Compute its value.

4. [8 points] You are trapped on an island, and decide to build a signal fire to alert passing ships. You start the fire with 200 pounds of wood. During the course of a day, 40% of the wood pile burns away (so 60% remains). At the end of each day, you add another 200 pounds of wood to the pile. Let  $W_i$  denote the weight of the wood pile immediately after adding the  $i^{\text{th}}$  load of wood (the initial 200-pound pile counts as the first load).
- a. [3 points] Find expressions for  $W_1$ ,  $W_2$  and  $W_3$ .
- b. [3 points] Find a closed form expression for  $W_n$  (*a closed form expression* means that your answer should not contain a large summation).
- c. [2 points] Instead of starting with 200 pounds of wood and adding 200 pounds every day, you decide to start with  $P$  pounds of wood and add  $P$  pounds every day. If you plan to continue the fire indefinitely, determine the largest value of  $P$  for which the weight of the wood pile will never exceed 1000 pounds.